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Stochastic Model Specification Search for Gaussian and Non-Gaussian State Space Models

by Sylvia Frühwirth-Schnatter and Helga Wagner

Discussion by Gabriele Fiorentini

University of Florence and Rimini Centre for Economic Analysis (RCEA)

• The paper is enjoyable and instructive

 In a nutshell: "the authors propose an ingenious parameterization of STS models that fits the variable selection approach of George and McCulloch"

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- The noncentered prameterization and a "classical" perspective
- Implementation of George and McCulloch variable selection method
- Motivations for stochastic model specification search in the STS framework

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Bayesian model discrimination in STS models

• STS models widely used in applied macroeconomics.

- Ideally macroeconomics should guide the time series model choice. Economic theories however rarely point to a unique specification, and discriminating between different possibilities can be difficult.
- Even in a simple trend plus noise decomposition the amount of uncertainty may be huge
 a) What model for the trend?
 - b) Deviations from trend should be a pure noise or a stationary autocorrelated short term component ?c) Identification of the component models

1) Model selection 2) Model identification

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Model selection

The Bayesian's answer to **model selection** is the posterior probability of model M_i :

$p(M_i|y) \propto f(y|M_i)p(M_i)$

Let $j = \arg \max_i p(M_i | y)$, then you can take $f(trend | y, M_j)$

I like more f(trend|y) which reflects the uncertainty faced by the researcher.

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Model Identification

Let M_i be a simple trend plus noise model in which the trend is an I(1) process without drift

$$y_t = \mu_t + \epsilon_t$$

$$\mu_t = \mu_{t-1} + \omega_t + \vartheta \omega_{t-1} \qquad \mathbf{0} \le \vartheta \le \mathbf{1}$$

there are infinitely many combinations of ϑ and the signal to noise ratio that are o.e.

Instead of imposing a specific identifying restriction on ϑ we could specify a prior distribution $f(\vartheta)$.

Then $f(trend|y, M_i)$ would reflect our uncertainty.

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The parameterization $\pm \sqrt{\theta}$ is discussed at length. It is argued that:

- Normal prior more suitable than IG under model uncertainty. Results are less sensitive to prior specification as the normal prior is less influential than IG prior.
 For θ is re-scaled χ² versus IG...
- Better mixing properties
 If mixing comes from sign switch...
- Bring important information about the hypothesis θ = 0
 It should help also under a classical approach...

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The Noncentered parameterization and classical statistics

What if one uses the same reparameterization under a standard ML approach.

This would change the constrained maximization of $L(\theta,...)$ into the unconstrained maximization of $L(\phi,...)$ (with $\phi^2 = \theta$).

Maybe, it would also transform a non standard testing problem into a standard one.

It doesn't work as $\frac{\partial L(\phi,...)}{\partial \phi}|_{\phi=0} = 0$ by construction.

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Implementation of the variable selection approach

There are different ways to implement George & McCulloch

The one adopted here requires the use of conjugate priors and when an indicator is equal to zero sets to zero also the corresponding parameter.

Could we use nonconjugate priors?

Does it make sense to set a normal prior with very small variance on $\sqrt{\theta}$ when the corresponding indicator is zero? Otherwise care must be exercised not the get reducible chains.

The method would clearly work for a trend+cycle+noise decomposition

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When the model space is large or moderate stochastic model search is the only solution.

There is no need to compute the whole posterior distribution

The stochastic search can work reasonably well even with chains of length smaller than the number of alternative models.

When the model space is small:

$$p(M_i|y) = \frac{f(y|M_i)p(M_i)}{\sum_{j=1}^{K} f(y|M_j)p(M_j)}$$

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Stochastic model search: extension

What if we have an unknown number of structural breaks at unknown dates.

The classic marginal likelihood approach is infeasible.

Adapting the stochastic model search to this case would be great.