

Central-Bank Communication and Policy Effectiveness*

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PRELIMINARY

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1 Why Communication Matters

The importance of communication strategy for policy effectiveness follows from a fundamental feature of the kind of problem that a central bank is called upon to solve. Central banking is not like steering an oil tanker, or even guiding a spacecraft, which follows a trajectory that depends on constantly changing factors, but that does *not* depend on the vehicle's own expectations about where it is heading. Because the key decisionmakers in an economy are forward-looking, central banks affect the economy as much through their influence on *expectations* as through any direct, mechanical effects of central bank trading in the market for overnight cash. As a consequence, there is good reason for a central bank to commit itself to a systematic approach to policy, that not only provides an explicit framework for decisionmaking within the bank, but that is also used to explain the bank's decisions to the public.

1.1 Central Banking as Management of Expectations

It is important for the public to understand the central bank's actions, to the greatest extent possible, not only for reasons of democratic legitimacy — though this is an excellent reason itself, given that central bankers are granted substantial autonomy in the execution of their task — but also in order for monetary policy to be most effective. For not only do expectations about policy matter, but, at least under current conditions, very little *else* matters. Few central banks of major industrial nations still make much use of credit controls or other attempts to directly regulate the flow of funds through financial markets and institutions. Increases in the sophistication of the financial system have made it more difficult for such controls to be effective, and in any event the goal of improvement of the efficiency of the sectoral allocation of resources stressed above would hardly be served by such controls, which (if successful) inevitably create inefficient distortions in the relative cost of funds to different parts of the economy.

Instead, banks restrict themselves to interventions that seek to control the overnight interest rate in an interbank market for central-bank balances (for example, the federal funds rate in the U.S.). But the current level of overnight interest rates *as such* is of negligible importance for economic decisionmaking; if a change in the overnight rate were thought to imply only a change in the cost of overnight borrowing for that one night, then even a large change (say, a full percentage point increase) would make little difference to anyone's spending decisions. The effectiveness of changes

in central-bank targets for overnight rates in affecting spending decisions (and hence ultimately pricing and employment decisions) is wholly dependent upon the impact of such actions upon other financial-market prices, such as longer-term interest rates, equity prices and exchange rates. These are plausibly linked, through arbitrage relations, to the short-term interest rates most directly affected by central-bank actions; but it is the expected future path of short-term rates over coming months and even years that should matter for the determination of these other asset prices, rather than the current level of short-term rates by itself.

Thus the ability of central banks to influence expenditure, and hence pricing, decisions is critically dependent upon their ability to influence market expectations regarding the *future path* of overnight interest rates, and not merely their current level. Better information on the part of market participants about central-bank actions and intentions should increase the degree to which central-bank policy decisions can actually affect these expectations, and so increase the effectiveness of monetary stabilization policy. Insofar as the significance of current developments for future policy are clear to the private sector, markets can to a large extent “do the central bank’s work for it,” in that the actual changes in overnight rates required to achieve the desired changes in incentives can be much more modest when expected future rates move as well.¹

Thus the public’s understanding, not only of what the central bank is currently doing, but of what it can be expected to do in the future, is critical for the effectiveness of policy. It might be nonetheless be argued that it should be enough for a central bank to systematic *follow* a sound policy, without also needing to explain it to the public. If one assumes rational expectations on the part of the public, it would follow that any systematic pattern in the way that policy is conducted should be correctly

¹There is evidence that this is already happening, as a result both of greater sophistication on the part of financial markets and greater transparency on the part of central banks, the two developing in a sort of symbiosis with one another. Blinder *et al.* (2001, p. 8) argue that in the period from early 1996 through the middle of 1999, one could observe the U.S. bond market moving in response to macroeconomic developments that helped to stabilize the economy, despite relatively little change in the level of the federal funds rate, and suggest that this reflected an improvement in the bond market’s ability to forecast Fed actions before they occur. Statistical evidence of increased forecastability of Fed policy by the markets is provided by Lange *et al.* (2001), who show that the ability of Treasury bill yields to predict changes in the federal funds rate some months in advance has increased since the late 1980s.

inferred from the bank's observed behavior. Yet while it would be unwise to choose a policy the success of which depends on its *not* being understood by the public — which is the reason for choosing a policy rule that is associated with a desirable rational-expectations equilibrium — it is at the same time prudent not to rely too heavily on the assumption that the public will understand policy perfectly regardless of the efforts that are made to explain it. Insofar as explanation of the policy rule to the public does no harm under the assumption of rational expectations, but improves outcomes under the (more realistic) assumption that a correct understanding of the central bank's policy commitments does not occur automatically, then it is clearly desirable for the central bank to explain the rule that it follows.

The advantages of a public target when the private sector must otherwise forecast future policy by extrapolating from experience are shown in a recent analysis by Orphanides and Williams (2005). In the Orphanides-Williams model, private agents forecast inflation using a linear regression model, the coefficients of which are constantly re-estimated using the most recent observations of inflation. The assumption of forecasting in this manner (on the basis of a finite time-window of historical observations) rather than a postulate of rational expectations worsens the tradeoff between inflation variability and output-gap variability that is available to the central bank. Allowing inflation variations in response to “cost-push” shocks for the sake of output-gap stabilization is more costly than it would be under rational expectations, because temporary inflation fluctuations in response to the shocks can be misinterpreted as indicating different inflation objectives on the part of the central bank. Orphanides and Williams then show that a credible commitment to a long-run inflation target — so that private agents do not need to estimate the long-run average rate of inflation, but only the dynamics of transitory departures from it — allows substantially better stabilization outcomes, though still not quite as good as if private agents were to *fully* understand the equilibrium dynamics implied by the central bank's policy rule. This provides a nice example of theoretical support for the interpretation given by Mervyn King (2005) and others of practical experience with inflation targeting, which is that tighter anchoring of the public's inflation expectations has made possible greater stability of *both* real activity and inflation.

Nor is there any reason to suppose that it suffices for a central bank to make clear the long-run average inflation rate that it intends to maintain, while allowing the public to reach its own conclusions about the nature of transitory departures

of the inflation rate from that long-run average. It is certainly true that anchoring expectations about the long-run average inflation rate is important, and that in itself is an important accomplishment. But the analysis of Orphanides and Williams also shows that even when private agents know the long-run average, but have to estimate the dynamics of transitory departures from it, the available tradeoff between inflation stabilization and output-gap stabilization is less favorable than it would be under rational expectations, *i.e.*, than it would be if one could rely on a correct understanding of the transitory dynamics. Thus there are in principle gains from an explicit commitment regarding this aspect of policy as well, and not simply trusting that people will be able to observe the pattern in one's behavior.

There is also a further, somewhat subtler, reason why explicit commitment to a target or policy rule is desirable, given the forward-looking behavior of the people in the economy that one seeks to stabilize. Even if one supposes that the private sector will fully understand whatever approach to policy the central bank takes, regardless of what it says about it, a public commitment to a rule can help policymakers to conduct policy in a way that achieves better outcomes. For is not enough that a central bank have sound objectives (reflecting a correct analysis of social welfare), that it make policy in a systematic way, using a correct model of the economy and a staff that is well-trained in numerical optimization, and that all this be explained thoroughly to the public. A bank that approaches its problem as one of optimization under *discretion* — deciding afresh on the best action in each decision cycle, with no commitment regarding future actions except that they will be the ones that seem best in whatever circumstances may arise — can still obtain a substantially worse outcome, from the point of view of its own objectives, than one that commits itself to follow a properly chosen policy *rule*. As Kydland and Prescott (1977) first showed, this can occur even when the central bank has a correct quantitative model of the policy tradeoffs that it faces at each point in time, and the private sector has correct expectations about the way that policy will be conducted.

At first thought, discretionary optimization might seem exactly what one would want an enlightened central bank to do. All sorts of unexpected events constantly occur that affect the determination of inflation and real activity, and it is not hard to see that, in general, the optimal level of interest rates at any point in time should depend on precisely what has occurred. It is plainly easiest, as a practical matter, to arrange for such complex state-dependence of policy by having the instrument setting

at a given point in time be determined only after the unexpected shocks have already been observed. Furthermore, it might seem that the dynamic programming approach to the solution of intertemporal optimization problems provides justification for an approach in which a planning problem is reduced to a series of independent choices at each of a succession of decision dates.

But standard dynamic programming methods are valid only for the optimal control of a system that evolves mechanically in response to the current action of the controller. The problem of monetary stabilization policy is of a different sort, in that the consequences of the central bank's actions depend not only upon the sequence of instrument settings up until the present time, but also upon private-sector expectations regarding future policy. In such a case, sequential (discretionary) optimization leads to a sub-optimal outcome because at each decision point, prior expectations are taken as *given*, rather than as something that can be affected by policy. Nonetheless, the predictable character of the central bank's decisions, taken from this point of view, do determine the (endogenous) expectations of the private sector at earlier dates, under the hypothesis of rational expectations; a commitment to behave differently, that is made credible to the private sector, could shape those expectations in a different way, and because expectations matter for the determination of the variables that the central bank cares about, in general outcomes can be improved through shrewd use of this opportunity. This is illustrated concretely in section 2, when I discuss the way in which policy should be conducted when the lower bound on short-term nominal interest rates constrains the way that policy can be conducted.

In general, the most effective policy (the best outcome, from among the set of possible rational-expectations equilibria) requires that policy be conducted in a *history-dependent* way, so that policy at any time depends not only on conditions then (and what it is considered possible to achieve from then on), but also on *past* conditions, even though these no longer constrain what it is possible to achieve in the present. While there is no benefit, at the time, from conducting policy in a way that is conditioned by the past, the *anticipation* that one would do so, at an earlier date, can have important beneficial effects on what policy can achieve at the earlier date. These benefits can make the subsequent losses worthwhile, as the example in the next section shows.

It is furthermore desirable, not simply that a central bank have a private intention of this sort, but that it be *publicly* committed to such a target. First, a public

commitment is likely to make it easier for the central bank’s policy deliberations to remain focused on the right criterion — the one with the property that systematic conformity to it leads to an optimal equilibrium — rather than being tempted to “let bygones be bygones.” And second, the benefits associated with commitment to a history-dependent policy depend entirely on this aspect of policy being *anticipated* by the private sector; otherwise, it *would* be rational to “let bygones be bygones.” There is no point to a secret commitment to the future conduct of policy in accordance with a history-dependent rule, while the private sector continues to believe that the central bank will act in a purely forward-looking fashion; thus the target should be explained as clearly as possible to the public, and shown to be guiding the bank’s decisions.

1.2 Communication About What?

Which specific types of communication by central banks are most important, in light of the objectives discussed above? It is possible to distinguish among at least four broad classes of issues, about which a central bank may consider revealing more or less to the public. The first is the central bank’s interpretation of *economic conditions*, including (perhaps) the central bank’s view of the outlook for the future, to the extent that this is shaped by factors other than the bank’s intentions with regard to policy. Central banks typically have large staffs devoted to collecting and analyzing information about current conditions in the economy, as an input into policy deliberations; and the accuracy of private-sector understanding of the state of the economy might be improved if the central bank were to reveal more about what it believes it has learned. A second topic is the content of the *policy decisions* that are made in the central bank about current operating targets. For example, as noted in the introduction, the Fed did not publicly confirm the existence of an operating target for the federal funds rate prior to 1994, whereas current practice is to release a statement immediately following each meeting of the FOMC, which, among other things, announces the operating target agreed upon at that meeting. A third possible kind of communication would be a description (which might be more or less explicit) of a *rule* in accordance with which policy decisions should be made in general. A fourth type of communication, much debated in the U.S. at present, makes statements about the *outlook for future policy*, in light of the current situation, without necessarily asserting that this illustrates a general rule that will always be followed.

These are all types of communication in which the public might be interested, and a general commitment to increased “transparency” might be taken to require greater explicitness about all of these matters. But the way in which “transparency” about one or another of these matters relates to the goal of more effective stabilization policy is somewhat different in each case. The first two types of communication are the ones that are least controversial among central bankers; to the extent that there are doubts about the desirability of saying more about the central bank’s analysis of current conditions, for example, this is largely connected to the way that the public may use this information to make inferences (rightly or wrongly) about the bank’s intentions regarding future policy. And it is in any event the effect of central-bank talk on the public’s expectations regarding future policy that is critical for the concerns introduced above. Hence it is communication about the way in which policy should be conducted in the future (the third and fourth types of communication listed above) about which I wish to speak here.

One might, first of all, make statements about the *targets* or objectives that future policy decisions will aim to achieve; ideally, one might imagine a full description of a *policy rule* to which the policy committee intends to conform. This is the ideal suggested by the theoretical literature, on the basis of the considerations summarized above. On the one hand, private-sector decisions depend, in principle, not just on near-term expectations, but on the expected state-contingent evolution of the economy far into the future; and one could only hope to communicate about what should happen in *all* of the relevant future states by specifying a general rule that will guide future policy. Thus to the extent that it were possible to formulate such a rule and genuinely intend to act in the way described, it would be desirable to make it public. Moreover, an optimal policy requires that the central bank commit itself to behave in a different way than would correspond to discretionary optimization. It is difficult to imagine institutionalizing such conduct other than through a conscious commitment to a particular rule inside the central bank itself; and if such a conscious intention exists, a public statement of the commitment is likely to help the policy committee to remember its intention.

In practice, policy rules can be formulated with varying degrees of specificity. Svensson and Woodford (2005) distinguish among “higher-level” and “lower-level” specifications. The highest-level description of a policy commitment is only a statement of the targets or goals that the institution is committed to pursue. An intermediate-

level description (a “specific targeting rule”) would specify a quantitative “target criterion” that the policy committee would seek to make its economic projections conform with each time that a policy decision is made. Finally, the lowest-level description (an explicit “instrument rule”) would state a precise rule for setting the policy instrument as a function of various other variables that the policy committee would monitor. The lowest-level description would be the most complete, and it might be considered the ideal (from the points of view both of precision and accountability) if it were practical to make so explicit a statement; but the higher-level descriptions are more likely to be things that actual central banks might be willing to commit themselves about, and commitments of these kinds represent very great advances over no commitment at all.

But what does any of this have to do with communication policy? The public commitment of a central bank to particular targets or to a particular policy rule will not be matters for routine, ongoing communication with the public that requires institutionalization. It is true that from time to time it will be appropriate to change the targets — as, for example, in the case of the change in the U.K. announced in December 2003, from an RPIX target of 2.5 percent per annum to a CPI target of 2.0 percent — but announcements of this kind are not what is generally understood by “communication policy.” Would communication policy be important, then, for a central bank that was actually able to commit itself to a policy rule?

There are two reasons why it surely would be. The first is the need for *verifiability* of the central bank’s commitment. One might imagine that the central bank’s seriousness about its declared targets could be ensured by checking whether they are met, without requiring the bank to say anything about *how* it ensures that they are met. For example, under a rumor that was widespread at one time, accountability was ensured in New Zealand by a “contract” with the Governor of the RBNZ according to which the Governor could be fired if realized inflation ever went outside a certain band. In practice, however, it makes more sense to monitor the existence of good-faith efforts to achieve the bank’s targets than to suppose that one can demand that the targets will actually be fulfilled at all times; and this will require communication by the central bank about the rationale for its policy decisions. Moreover, to the extent that optimal target criteria involve the expected paths of variables that cannot yet be directly measured, as is typically the case, it is appropriate to check, not whether the *actually realized* values satisfy the target criterion, but whether it

would have been reasonable for the central bank to *expect* them to satisfy the criterion at the time of its policy decision. This requires the central bank to discuss the projections on the basis of which the policy decision was made.

The second reason is that the state-contingent policy that the central bank follows (and may wish to be understood to follow) may be too complex to explain in detail in any one-time official statement of its “policy rule.” It may nonetheless be possible to *illustrate* the consequences of the bank’s approach to policy deliberations by showing how the particular situations that have already arisen were analyzed; over time, the observation of a sufficient number of such cases should help the private sector to some degree of understanding of the central bank’s implicit “rule.” (The chances of this occurring, of course, are vastly greater in the case that the bank does itself seek to base its decisions on a stable set of principles, despite the varying kinds of information that are considered on different occasions, and in the case that it explains its decisions each time by reference to those same principles.) But this approach to making public the systematic character of policy will depend on a commitment to frequent communication about ongoing policy deliberations within the bank. Ideally, such communication will be regular, detailed, and structured, as in the case of the Inflation Reports of the inflation-forecast targeting central banks (discussed further in section 3).

A somewhat different way in which central-bank talk can convey information about future policy is through direct statements about the current outlook for policy. Such statements — illustrated by the comments that have recently been included in the post-meeting statements of the FOMC in the U.S. (discussed further in section 2) — fall considerably short of stating a general rule for the conduct of policy, and are likely to refer only to future policy over a fairly short horizon. They can, however, be much more specific about matters such as how the policy instrument will be set than descriptions of the bank’s general approach to policy are likely to be.

There are a number of questions that may be raised about the desirability of this kind of communication. One point of view — once fairly common among central bankers, though less common now — would question whether it is actually desirable to increase the degree of precision with which the markets are able to anticipate the actions of the central bank, arguing that market interventions by the central bank will be more *effective* to the extent that the bank is able to *surprise* the markets. The idea, essentially, is that unanticipated trading by the central bank should move

market rates by more, owing to the imperfect liquidity of the markets. Instead, if traders are widely able to anticipate the central bank's trades in advance, a larger number of counter-parties should be available to trade with the bank, so that a smaller change in the market price will be required in order for the market to absorb a given change in the supply of a particular instrument.

But such an analysis assumes that the central bank better achieves its objectives by being able to move market yields more, even if it does so by exploiting temporary illiquidity of the markets. Yet the temporarily greater movement in market prices that is so obtained occurs only because these prices are temporarily less well coupled to decisions being made outside the financial markets. Hence it is not at all obvious that any actual increase in the effect of the central bank's action upon the economy – upon the things that are actually relevant to the bank's stabilization goals – can be purchased in this way.²

A second reason to question the need for central-bank talk about the outlook for future policy would assert that it should be redundant, if a central bank is committed to a policy rule, as it ought to be. The general rule, once stated, should not require further discussion of what the outlook for policy might be on particular occasions. One answer would be that communication of this kind could still be useful as a halfway measure, for those central banks that are reluctant to commitment themselves to targets or rules in general, but nonetheless be willing to commit themselves occasionally to an *ad hoc* departure from fully discretionary policy. In fact, communication of this kind has been used most notably thus far by central banks such as the U.S. Federal Reserve and the Bank of Japan,³ which have *not* been willing to explicit themselves to quantitative inflation targets.

But discussion of the outlook for policy is likely to play a useful role even within the context of an ideal targeting regime. In practice, the general rule that it would be possible to state in advance would be a rule of one of the “higher-level” types, and not an explicit instrument rule. There would thus be considerable room to give further information about the likely path of the policy instrument on particular occasions,

²I develop this point in more detail in Woodford (2001), where a simple model of policy effectiveness with incomplete market participation is presented.

³I discuss recent policy signalling by the Fed in section 2. On recent policy signalling by the Bank of Japan, see Bernanke *et al.* (2004), Fujiki and Shiratsuka (2002), Iwamura *et al.* (2004) and Oda and Ueda (2005).

that would neither contradict nor be made unnecessary by the bank's commitment to its general policy rule. Such communication would help to flesh out the concrete implications of the general rule, and increase the ability of the private sector to make correct inferences about the consequences of the rule for the future evolution of the economy. This kind of amplification of the general policy rule is likely to be especially useful when unusual circumstances arise, so that the implications of the general policy rule for circumstances of that kind might not be at all apparent simply from observation of the bank's past behavior. The situation discussed in the next section — where the Federal Reserve found itself at least potentially constrained by the zero lower bound on nominal interest rates, though this constraint had been irrelevant for more than fifty years — provides a good example of such an occasion.

A further argument for the desirability of communication about the outlook for future policy — and one in no way tied to unusual circumstances — follows from the history-dependence of an optimal policy commitment. Optimal policy requires not only that the central bank commit itself to a particular rule of conduct, but that the rule be history-dependent: it must take account of past conditions, even some that no longer matter for an evaluation of what it would be possible to achieve from now on. Hence any institutionalization of an optimal rule must involve keeping some record of past conditions. It is furthermore worth noting that what matters is not what the past was actually like (as viewed from the future, when the history-dependent policy action is to be taken), but how matters *appeared* then, as this is what would determine the value at the earlier time of being able to shift expectations regarding future policy.⁴ Thus implementation of an optimal policy requires that a record be kept of how matters appeared to the policy committee in the past, and that those past views condition the later policy decision. And while history-dependent policy requires only that there exist an internal record, the *benefits* of history-dependence depend on its being understood by the public; this makes a public statement about the aspects of the current situation that should change future policy deliberations appropriate.

⁴In optimal policy calculations like the ones discussed in the next section, the history-dependence of optimal policy results from the presence of lagged Lagrange multipliers in the first-order conditions that characterize the optimal state-contingent evolution of the economy. The lagged values of these Lagrange multipliers depend on the decision problem faced by the central bank *at its last decision point*. For further discussion, see Woodford (2003, chap. 7) and Svensson and Woodford (2005).

There are various ways in which the relevant aspects of past deliberations might be encoded, and in which those records might be used in subsequent deliberations. But one fairly straightforward one — which would make it especially easy for the public to understand the consequences for future policy — would be to indicate at the earlier date the future policy that should be expected to be implemented later, in the absence of developments unforeseen at that time. The policy committee would then be committed to actually implement the policy announced earlier, unless circumstances changed in ways not previously foreseen. Deciding policy in advance (to this extent) would be an obvious way of allowing the policy committee to internalize the effects of anticipations of its later policy, and making public the committee's forecast of future policy would be an obvious way of making clear the expectations regarding future policy that should follow from the intention to make policy history-dependent. Of course, in order to prevent such an advance commitment from implying a non-state-contingent (and hence suboptimal) rule of conduct, it would be important to specify the assumptions regarding economic developments under which the forecast about future policy had been made, so that the nature of the contingency of the commitment would be clear.

2 Signaling Future Policy Near the Interest-Rate Lower Bound

A case in which the benefits of being able to steer expectations regarding the future conduct of policy, other than through current policy actions alone, are especially clear is in the case in which overnight interest rates are already as low as it is possible or desirable to make them, while underutilization of productive capacity and/or unduly low inflation continue to suggest a need for further monetary stimulus. Japan, where the overnight rate (call rate) has been at zero almost continuously since 1999, yet deflation continues, provides an obvious example of the possibility of such a situation. But the U.S. faced a similar situation, or at least the risk of one, in the spring and summer of 2003, as the federal funds rate operating target was reduced to only one percent, while the strength of the recovery remained doubtful and inflation remained lower than the Fed was entirely comfortable with.

Does monetary policy become impotent when the zero lower bound is reached, as

classic analyses of the possibility of a “liquidity trap” in static models would suggest? Eggertsson and Woodford (2003) show that the answer is yes, in the context of an explicit general-equilibrium model of the transactions demand for money with sticky prices, if monetary policy is understood to consist solely of various ways in which the monetary base might be expanded through current open-market operations, without any change in the way in which monetary policy is expected to be conducted in the future.⁵ But they also show that changes in the expected conduct of monetary policy in the future — after real conditions change, so that the policy that would be preferred at the time, but for the need to fulfill earlier commitments, would be one in which nominal interest rates would be well above zero — can have a very substantial effect on inflation and real activity during the period in which the zero bound is a binding constraint. This indicates the possibility of substantial benefits from signalling that future policy will be conducted in a different way than might otherwise have been expected, simply as a result of the economy’s having been temporarily constrained by the interest-rate lower bound.

2.1 An Optimal Policy Commitment when the Lower Bound Binds

It is worth recapitulating some of the details of the analysis of optimal policy by Eggertsson and Woodford (2003), as a basis for discussion of the recent use of communications policy in both the U.S. and Japan. The exposition is simplest if we proceed directly to a log-linear approximation to their intertemporal equilibrium model with Calvo-style staggered price-setting. In this approximation (which, except for the imposition of the zero bound, is identical the one used in studies such as Clarida *et al.*, 1999), inflation π_t and the output gap x_t are determined by a pair of equations

⁵This analysis extends the discussion of Krugman (1998) to include a more developed treatment of the dynamics of price adjustment, the connection between interest-rate policy and the generation of inflationary expectations, and the consequences of alternative forms of open-market operations.

each period,⁶

$$\pi_t = \kappa x_t + \beta E_t \pi_{t+1}, \quad (2.1)$$

$$x_t = E_t x_{t+1} - \sigma [i_t - E_t \pi_{t+1} - r_t^n], \quad (2.2)$$

where κ, σ are positive coefficients, and $0 < \beta < 1$ is the utility discount factor, i_t is the riskless short-term (one-period) nominal interest rate, and r_t^n is the natural (real) rate of interest, that evolves exogenously as a result of real disturbances. The interest rate i_t is assumed to be the instrument of monetary policy, and is here treated as under the direct control of the central bank. We may then suppress the equations of the model involving the demand for base money. However, it is important to note that the interest rate will satisfy

$$i_t \geq 0 \quad (2.3)$$

no matter how much base money is supplied; this lower bound is the constraint on policy with which we are here concerned.

Let us suppose that the objective of policy is to minimize a discounted loss function of the form

$$E_0 \sum_{t=0}^{\infty} \beta^t [\pi_t^2 + \lambda x_t^2], \quad (2.4)$$

with some weight $\lambda > 0$. It follows from equations (2.1) – (2.2) that as long as $r_t^n \geq 0$ at all times, one possible rational-expectations equilibrium is one in which inflation and the output gap are both zero at all times, and in such a case, this is obviously the equilibrium that minimizes the loss function (2.4), and so is optimal. But it is possible for real disturbances to cause the natural rate of interest to be temporarily negative.⁷ In such a case, the zero-inflation equilibrium is no longer a possibility. (Note that this equilibrium requires that $i_t = r_t^n$ at all times, so that (2.3) is satisfied only if $r_t^n \geq 0$ at all times.)

⁶Equation (2.1) is here written without the “cost-push shock” term that plays a central role in the analysis of optimal policy in Clarida *et al.* The issue with which we are here concerned (the possible difficulties for policy created by the zero bound) is not one for which the existence of a “cost-push” term is important, whereas the existence of fluctuations in the natural rate of interest r_t^n is instead critical. The optimal policy rule derived by Eggertsson and Woodford (2003), however, is also optimal in the presence of “cost-push shocks” of the kind hypothesized by Clarida *et al.*

⁷This is Krugman’s (1998) analysis of the situation of the Japanese economy since the mid-1990s. See also Woodford (2003, chap. 4) for discussion of some of the kinds of real factors that can shift the natural rate of interest.

Given that the pursuit of zero inflation at all times would be optimal in the event that the lower bound on interest rates were never a problem, one might suppose that even given the possibility of an occasionally binding lower bound, it would be optimal to pursue zero inflation at all times, *if* the interest-rate lower bound allows it. But this is not true. As an illustration, consider the particular kind of real disturbance analyzed in the numerical example of Eggertsson and Woodford. The “normal” (long-run average) level for the natural rate of interest is $\bar{r} \equiv \beta^{-1} - 1 > 0$. However, at some date, an unexpected disturbance temporarily lowers the natural rate to a level $\underline{r} < 0$. There is then a probability $0 < p < 1$ each period that “fundamentals” revert to their normal state, so that $r_t^n = \bar{r}$ again, and in this case, the natural rate of interest is expected to equal \bar{r} indefinitely (there are no further disturbances). With probability $1 - p$, instead, the low-natural-rate state will continue in the following period, conditional on the natural rate remaining at \underline{r} in the current period.

In this case, under the hypothesized policy, the central bank will achieve zero inflation from period T onward, where T is the random date at which fundamentals revert to their normal state. This will be associated with a constant output gap of zero, and a constant nominal interest rate equal to $\bar{r} > 0$. Prior to this date, inflation will equal the same rate $\underline{\pi}$ each period, the output gap will equal the same value \underline{x} , and the nominal interest rate will equal the same value \underline{i} ,⁸ where these constant values satisfy

$$\underline{\pi} = \kappa \underline{x} + \beta(1 - p)\underline{\pi}, \quad (2.5)$$

$$\underline{x} = (1 - p)\underline{x} + \sigma[\underline{r} + (1 - p)\underline{\pi} - \underline{i}], \quad (2.6)$$

as a result of equations (2.1) – (2.2), together with the requirements that

$$\underline{\pi} \leq 0, \quad \underline{i} \geq 0, \quad (2.7)$$

and that at least one of the inequalities in (2.7) must hold with equality. (The central bank achieves the zero inflation target at dates prior to T , unless the zero bound prevents the inflation rate from being raised to zero.)

An equilibrium of this form exists as long as

$$(1 - p) \left(\beta + \frac{\kappa\sigma}{p} \right) < 1, \quad (2.8)$$

⁸Here I restrict attention to the Markovian (minimum-state-variable) equilibrium consistent with the hypothesized policy. Note that when this equilibrium exists, it represents at least *one* possible outcome, and the fact that it may be very bad indicates the problem with this approach to policy.

i.e., as long as the degree of persistence of the disturbance is not too great. One can easily show that under the assumption that $\underline{r} < 0$, it is the lower bound on interest rates that is binding in (2.7), and the solution is given by

$$\underline{\pi} = \frac{\underline{r}}{(\kappa\sigma)^{-1}p[1 - \beta(1 - p)] - (1 - p)} < 0, \quad \underline{x} = \frac{1 - \beta(1 - p)}{\kappa}\underline{\pi} < 0, \quad (2.9)$$

together with $\dot{z} = 0$. Thus deflation and output below the natural rate continue for as long as the disturbance to fundamentals does; even if prices are revised fairly often on average, the binding lower bound on interest rates can result in a slump that lasts for years. Furthermore, (2.9) implies that even a very mildly negative value for the natural rate of interest can result in very severe deflation and contraction of real activity. Note that if the left-hand side of (2.8) is close enough to 1 (and there is no reason why it may not be), the rate of deflation and the size of the negative output gap in (2.9) become arbitrarily large, regardless of the degree to which \underline{r} is less than zero.⁹

The contractionary effects may be quite large, due to a chain of circular causation. A real interest rate above the natural rate (owing to the zero bound) causes a negative output gap and deflation prior to period T . The anticipation of these effects, in the contingency that the natural rate continues to be negative in the following period, then depresses demand further and creates even stronger deflation in any period prior to T , owing to the effects of expectations $E_t\pi_{t+1} < 0, E_tx_{t+1} < 0$ in equations (2.1) – (2.2). The anticipation of these even stronger deflationary and contractionary effects causes still greater deflation and contraction, and so on, in a cumulative process that does not even converge unless (2.8) holds.

It is crucial in the above reasoning that the central bank is expected to target zero inflation again as soon as this becomes possible. While this would in fact make sense *ex post* — and so would be the outcome in a Markov equilibrium with discretionary optimization by the central bank — a better outcome is possible if the central bank commits to behave otherwise once fundamentals revert to their normal state. This can be seen if we repeat the above calculations, but assume that the central bank will bring about an inflation rate $\bar{\pi} > 0$ (and an associated output gap $\bar{x} > 0$) in period

⁹Of course, for a large enough rate of deflation and departure from the natural rate of output, the local approximations in (2.1) – (2.2) cease to be accurate; but this suffices to show that the departures from the zero-inflation steady state need not be *small*, for if they were small the local approximations would be valid and equations (2.9) would be approximately correct.

T . Under this variation on our assumptions, the solution for $\underline{\pi}$ in (2.9) generalizes to¹⁰

$$\underline{\pi} = \bar{\pi} + \frac{\underline{r} + \bar{\pi} + p\sigma^{-1}[\bar{x} - x^{ss}(\bar{\pi})]}{(\kappa\sigma)^{-1}p[1 - \beta(1 - p)] - (1 - p)}, \quad (2.10)$$

where $x^{ss}(\bar{\pi}) \equiv (1 - \beta)\kappa^{-1}\bar{\pi}$ is the steady-state output gap associated with steady-state inflation rate $\bar{\pi}$.

In the case that \bar{x} is increased along with $\bar{\pi}$ to the extent that it would in the case of a permanent commitment to the inflation target $\bar{\pi}$, the multiplier effect of an increase in the long-run inflation target $\bar{\pi}$ on the inflation rate $\bar{\pi}$ during the “liquidity trap” is given by

$$\frac{\partial \underline{\pi}}{\partial \bar{\pi}} = 1 + \mu,$$

where $\mu > 0$ is the (possibly very large) multiplier $-\partial \underline{\pi} / \partial \underline{r}$ implied by equation (2.9). There is a correspondingly large effect of a commitment to target an inflation rate $\bar{\pi} > 0$ on the value of \underline{x} as well. Thus a commitment to a future inflationary policy can mitigate the effects of the zero lower bound, as argued by Krugman (1998). In the forward-looking model of inflation and output determination used here, these effects are quite large, owing to the same chain of circular causation as above, but now operating in the opposite direction (a “virtuous circle”).

However, the optimal policy commitment (in order to minimize (2.4) is not a simple commitment to a higher long-run inflation target. The effects just discussed on inflation and output while the zero lower bound binds depend only on $\bar{\pi}$ and \bar{x} being delivered in period T , the *first* period in which the natural rate of interest is again positive; there is no need to commit to *continued* inflation forever, and this will instead lead to unnecessary distortions in the long run. Eggertsson and Woodford (2003) show that the optimal policy involves a commitment to the creation of a modest inflationary boom in period T , and then stabilizing the price level shortly thereafter (*i.e.*, returning to a long-run inflation rate of zero), at a level slightly higher than the one that would have been reached in the absence of the disturbance.¹¹

¹⁰Equation (2.10) applies as long as $\bar{\pi} \leq -\underline{r}$, so that the zero bound continues to bind when $r_t^n = \underline{r}$.

¹¹Jung *et al.* (2005) reach a similar conclusion in the case of different assumed dynamics for the natural rate of interest. Adam and Billi (2003) characterize optimal policy in the same model in the case of continuing stochastic fluctuations in the natural rate that cause the zero bound to bind periodically.

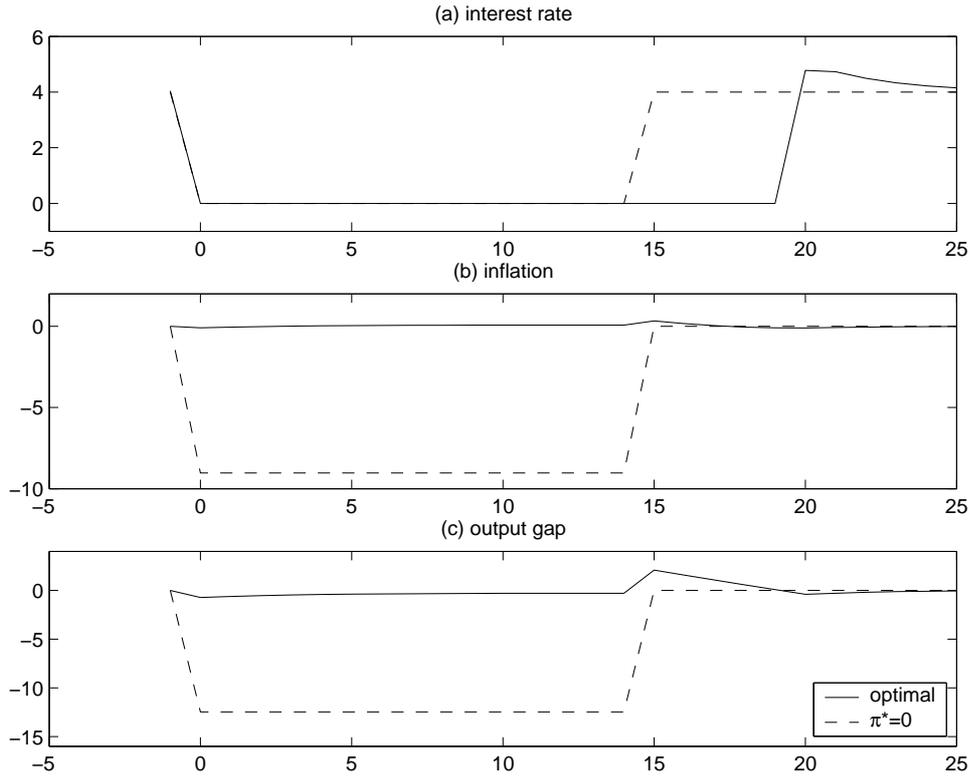


Figure 1: Comparison of state-contingent paths under two alternative monetary policies, in the case that the natural rate of interest is negative for 15 quarters. (Source: Eggertsson and Woodford, 2003)

This is illustrated in Figure 1, which shows the paths of the nominal interest rate, the inflation rate, and the output gap under the optimal state-contingent policy commitment (for particular numerical parameter values discussed by Eggertsson and Woodford), in the case that T is exactly 15 quarters after the onset of the real disturbance. The figure also shows the paths of all three variables in the case of a commitment to zero inflation (or discretionary optimization). While the creation of the inflationary boom (by keeping interest rates low for five more quarters, rather than immediately raising them to the level that would be required to achieve price stability immediately at date T) results in mild distortions after date T , these are only temporary (as price stability and a zero output gap are achieved fairly soon), and are quite mild relative to the size of the distortions prior to date T that are thereby avoided. The strong effect of the commitment to subsequent reflation of the

economy occurs because of the chain of circular causation just discussed.¹²

This numerical example illustrates several points of more general importance. First, it shows how a credible commitment regarding the future conduct of policy can, at least in principle, greatly expand a central bank's ability to achieve its stabilization objectives. But in addition, it shows that the an optimal commitment requires not only that the central bank pledge to behave in a different way than would a discretionary optimizer; the conduct of policy must also be *history-dependent*. For the inflation rate that should be targeted once the natural rate of interest is positive is not the one that the central bank *always* targets in the case of fundamentals of that kind; rather, the central bank should temporarily behave differently because of what the economy's situation *has been* in the recent past, even though those circumstances no longer affect what it would be possible for policy to achieve from now on. As I have discussed above, this history-dependence of the optimal policy commitment strengthens the case for explicit discussion by the central bank of the way in which current conditions change the outlook for future policy. If it were desired simply to *always* target an inflation rate $\bar{\pi} > 0$, then it might not be necessary for the central bank to talk about this while in the liquidity trap; one might suppose that the central bank's long-run inflation target would already have been learned by the private sector from its previous behavior, and that people might confidently expect the central bank to return to the pursuit of this target once circumstances allowed it to be achieved, without any need for comment to that effect. But if it is desired that the public understand, while policy is constrained by the zero bound, that future policy will be *different* from what it usually is under similar circumstances, because of the current difficulties, then it is reasonable to suppose that the central bank may need to discuss this, rather than expecting this to be obvious from past experience. The case will be even stronger if the circumstances under which the zero bound becomes a constraint are fairly unusual.

It is also worth noting that the advantages of commitment to a history-dependent future policy do not depend on reaching the zero bound. It is simply important that there be *some* lower bound on the level of short-term nominal interest rates that the

¹²These effects are quite strong because it is assumed in the example that there is only a ten percent chance each quarter that fundamentals will revert to the normal state. Thus at any point in time while the natural rate of interest is negative, it is expected that this situation is likely to persist for two or more additional years.

central bank is willing to target; none of the analysis just sketched depends on there being satiation in money balances when this bound is reached. In the analysis of Eggertsson and Woodford, there is no need for history-dependent policy unless there is some state in which the zero bound binds; but that is because they assume there is no *other* obstacle to lowering interest rates. If (as was arguably the case for the Fed in 2003) there is a positive level of interest rates i^l below which the central bank does not wish to go, a similar analysis applies in the case of this lower bound, except that now history-dependent policy becomes valuable if the natural rate of interest ever drops below i^l , which is even more likely to occur if i^l is positive.¹³ Regardless of where the lower bound lies, a commitment to lower interest rates later can substitute, at least partially, for being able to lower interest rates immediately, so that history-dependent policy can relax the constraint implied by the lower bound.

2.2 Policy Signalling in Practice

The situation faced by the U.S. Federal Reserve in the summer of 2003 was arguably of the sort contemplated in the above analysis (though the model used in the calculations is obviously an extreme over-simplification). The federal funds rate operating target had been reduced to 1.0 percent by June of that year, and (at least according to speculation in financial markets and in the press) the FOMC may have been reluctant to move lower than that. Nonetheless, inflation remained low; according to the minutes of the August 2003 meeting of the FOMC, inflation was “already near the low end of what some members regarded as an acceptable range,” and “a number of members expressed the view that some further disinflation was probable over the year ahead.” While the committee was at least guardedly optimistic about real growth over the next year, it was believed that a substantial period of growth faster than the economy’s potential growth rate would be needed to close “the economy’s currently wide output gap.”

Because of the risk of undesired further declines in inflation — that posed a particular risk insofar as once inflation *expectations* also fell, the level of real interest rates associated with the nominal interest rate floor would become an even higher

¹³The analysis can similarly be generalized to the case of an objective function in which the optimal inflation rate is assumed to be some positive inflation rate π^* , rather than zero. In this case, history-dependent policy is needed only if the natural rate of interest sometimes falls below the level $i^l - \pi^*$.

one — the FOMC did not wish to tighten policy, despite the improving outlook for real activity. In this regard, it was not judged to be enough that they leave the funds rate target at one percent; for, as explained in section 1, it is primarily the *expected future path* of the funds rate (and other short rates tied fairly closely to it) that affects spending and pricing decisions, rather than the current level of the funds rate. And there was concern that the public’s expectations regarding the future path of interest rates could move sharply upward as news about the real economy improved, because of the way in which the FOMC had typically responded to improvements in real activity in the past (as described, for example, by the “Taylor rule”). These expectations, if allowed to respond in that apparently reasonable way, might slow the recovery of real activity and plunge the U.S. economy into deflation.

The minutes of the August meeting indicate the committee’s concern with the recent evolution of market expectations, as indicated by long-term bond yields. The minutes discuss the “dramatic” increase in the ten-year Treasury yield in particular that had occurred in July (see Figure 2, below). “The increase appeared to be based on a number of factors, including investors’ interpretation of the Chairman’s congressional testimony, the release of Committee members’ relatively bullish economic projections, and incoming news regarding the economy and corporate earnings that was seen as signaling a more likely upturn in economic growth,” as a result of which the markets were evidently anticipating that increases in the funds rate might come as early as the fall. While the minutes do not clearly identify the reason for the FOMC’s decision to introduce an explicit comment on the likely nature of future policy into its post-meeting statement on this occasion, it seems likely that their concern with movements in long-term bond yields on the basis of speculation about their future policy decisions was an important element in the decision to not leave the judgment of the market about this matter to guesswork.¹⁴

After reporting that the funds rate operating target would remain at 1.0 percent for another month, and assessing the “balance of risks” (“The Committee judges that, on balance, the risk of inflation becoming undesirably low is likely to be the predominant concern for the foreseeable future”), the statement included a final sentence of

¹⁴Concern about the effectiveness of their communication strategy was also indicated by the fact that the committee scheduled a meeting for September, prior to the next policy decision, to reconsider “its practices regarding the communication of its policy decisions and its assessment of the risks to its objectives.”

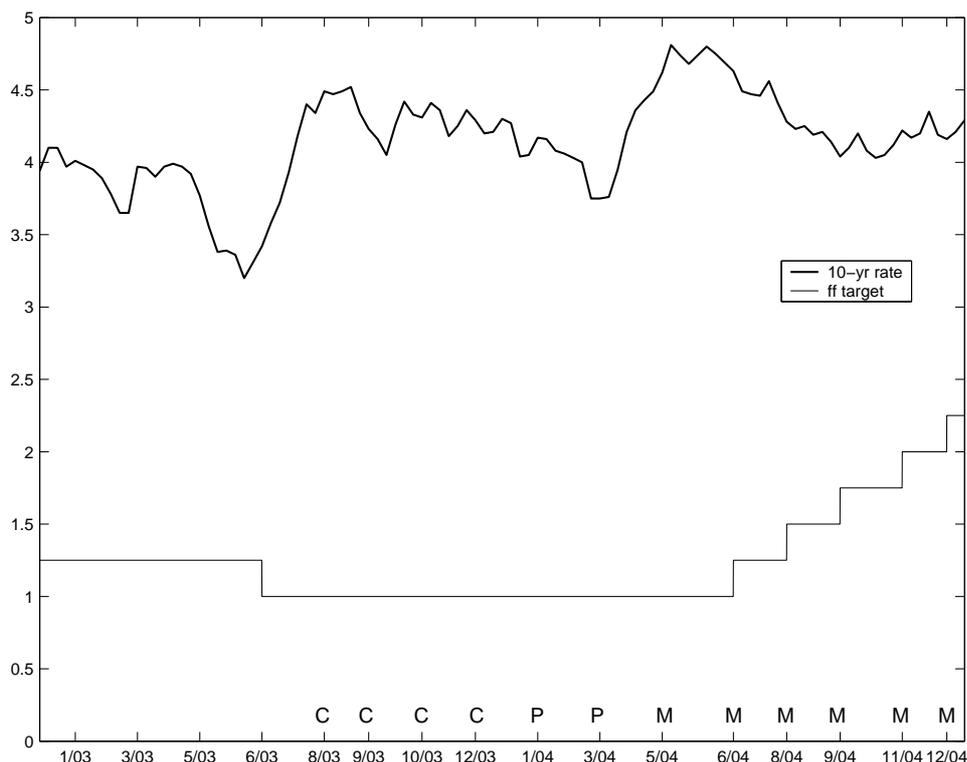


Figure 2: The federal funds rate target and the 10-year Treasury rate. Comments about likely future FOMC policy in post-meeting statements are indicated by letter codes: C = “considerable period”, P = “patience”, M = “measured pace.”

a new type: “In these circumstances, the Committee believes that policy accommodation can be maintained for a considerable period.” While no outright commitment was made, the minutes indicate that the members in favor of this statement believed it likely “that the Committee would want to keep policy accommodative for a longer period than had been the practice in past periods of accelerating economic activity.”

In fact, the committee acted as though they regarded themselves as committed not to raise rates, without some months of advance warning. The “considerable period” language was repeated in the statements released following each of the next three meetings as well (*i.e.*, through the end of 2003).¹⁵ When the likelihood of interest-rate increases by the middle of 2004 became apparent, the fact that the

¹⁵The dates on which statements have been released containing various types of language regarding likely future policy are indicated in Figure 2 by the codes ‘C’, ‘P’, and ‘M’. The code ‘C’ indicates a reference to maintaining accommodation for a “considerable period.”

funds rate would not remain at 1.0 percent indefinitely was indicated by dropping the “considerable period” language.¹⁶ Instead, the final sentence of the statement released following the meeting at the end of January 2004 said that “the Committee believes that it can be patient in removing its policy accommodation.” According to the minutes, “all the members agreed that a change in wording was desirable, not to signal a policy tightening move in the near term, but rather to increase the Committee’s flexibility to take such an action when it was deemed to be desirable and to underline that any such decision would be made on the basis of evolving economic conditions.” This language was included again in the March 2004 statement, while the May 2004 statement instead indicated that “the Committee believes that policy accommodation can be removed at a pace that is likely to be measured.” Even at this meeting, the funds rate target was not raised; but notice had been given that it *would* now be raised, albeit at a “measured pace.” The funds rate target was indeed raised, beginning at the next meeting; it has now (at the time of writing) been raised by two full percentage points, through a succession of quarter-point increases at eight successive meetings. Throughout this period of steady increases, the post-meeting statements have continued to include the reference to expecting to remove policy accommodation at a “measured pace.”

What has the new policy of commenting on the likelihood of future changes in the funds rate target achieved? The “considerable period” language seems to have been intended to influence market expectations in a way that would stimulate additional spending — higher spending, that is, than would have occurred if expectations had been allowed to change in the direction that it was feared they would in the absence of such assurances from the FOMC. As in the scenario described by Eggertsson and Woodford, a statement that interest rates would be kept low for a longer period of time was able to substitute for an immediate cut in rates.¹⁷ The signal furthermore seemed

¹⁶The commitment to keep rates low “for a considerable period” had already been qualified in the December 2003 statement, by the inclusion of a reference tying this policy to continued low inflation and resource “slack”.

¹⁷There is no indication in the minutes that the FOMC did not believe that interest rates could ever be cut below one percent. But for whatever reason, no further cut in the funds rate target was made, despite the desire to head off further disinflation, and to signal to the markets that policy would not be tightened as much as was widely believed. In discussing policy in the summer of 2003, Governor Donald Kohn speaks of a funds rate target of zero as having “uncertain consequences,” and says that signalling about future policy instead “seemed to be the less-risky way” to stimulate

to be effective. Governor Ben Bernanke, speaking the following year, argued that “the language of the statement in August 2003 and subsequent meetings persuaded the markets that an autumn tightening was not in the cards, and market expectations adjusted accordingly. Crucially, this change in expectations resulted in lower interest rates at all maturities, a development that helped support the expansion in the latter part of last year” (Bernanke, 2004). The decline in the 10-year bond rate following the introduction of this commitment is shown in Figure 2. While bond yields move for a variety of reasons, this decline even as fears of deflation dissipated and the outlook for the real economy continued to improve suggests that the new communication policy had its intended effect on expectations.¹⁸

The eventual transition to a higher level for the funds rate has also been managed in a way that has involved few surprises for the markets, and that has not resulted in a bond market rout, sending long rates to levels greater than those consistent with the intended medium-term level of interest rates. As it became clear in the spring of 2004 that the commitment to maintain rates at their existing (historically low) level was about to end, with no indication from the Fed as to how dramatic a change in policy might be coming, long bond yields again rose fairly sharply. But the introduction of the commitment to a “measured pace” in May allowed long rates to decline again, as shown in Figure 2. Since then, it has been possible to increase the funds rate target by a total of two percentage points, while the 10-year bond rate remains (at the time of writing) at about the same level as it was late in 2003, and below the level that it had reached in the summer of 2003, prior to the introduction of the “considerable period” language. This sort of outcome is not especially paradoxical when increases in the funds rate target occur within the context of a funds rate path that was already fairly predictable, so that the increases themselves cause no change in market expectations about the likely level of interest rates over the next several years (and may actually contribute to *lower* expectations regarding nominal interest rates some years out, insofar as they confirm that the central bank will be vigilant to contain inflation). Bernanke (2004) suggests that the new communications policy

demand (Kohn, 2005). This suggests that there was indeed a reluctance to cut the funds rate target, at least given the existence of an alternative lever of policy.

¹⁸Discussing the same period, Governor Kohn (2005) states “I would judge the outcome to have been successful. We did influence rates to better reflect the actual path of policy,” with a good outcome for the economy as well.

has also likely contributed to a recent decline in “overall financial market volatility ... by reducing the uncertainty surrounding the future course of policy.”

The primary difficulty associated with this policy has been some degree of discomfort among at least some members of the FOMC with the degree to which statements of this kind constrain the policy decisions that can be made at later meetings.¹⁹ Of course, one of the *advantages* of such statements that I have suggested above is precisely that they can constrain a policy committee to not behave in the way that would otherwise seem appropriate *ex post*; such constraint can be desirable, because of the benefits that flow from being anticipated to conduct policy in a history-dependent fashion. For example, in the case of the optimal state-contingent policy depicted in Figure 1, it would be important that the central bank feel itself constrained not to raise interest rates in quarter 15, despite the fact that it has learned that (relatively unexpectedly) the natural rate of interest has returned to its normal, positive level, and despite the fact that failing to do so means creating a mildly inflationary boom. Policymakers may be uncomfortable with such behavior because they are reasoning like discretionary optimizers — in which case they are not wrong to expect to be constrained by the commitment, but they are wrong to think they choose not to constrain themselves, at least in the case that the constraint can be expected to be understood by the public.

But in all likelihood, the discomfort is not solely due to a failure to understand the logic of Kydland and Prescott (1977), but also to frustration with the crudeness of the kinds of commitments that can be made using such simple statements as the ones just paraphrased. The signals that have been given thus far through the post-meeting statements all attempt to say something about the likely path of the funds rate for the next several months; they refer (in a way that is open to interpretation) to rates of change and periods of time, but, except for the constant qualification that the statement is only an indication of “likely” policy, they do not speak of the way in which future policy should be *contingent* on circumstances that are not already evident. If the statements are interpreted as *commitments* to particular non-state-

¹⁹For example, the minutes for the May 2004 meeting, at which the “measured pace” language was introduced, reports that “a number of policymakers were concerned that such an assertion could unduly constrain future adjustments to the stance of policy should the evidence emerging in coming months suggest that an appreciable firming would be appropriate,” though all members eventually endorsed the language adopted.

contingent paths for the funds rate — albeit commitments that specify the path only for a fairly short distance ahead — then they are likely to constrain policy in ways that are not fully ideal.

For while an optimal policy commitment will generally imply that policy should be *history-dependent*, as stressed above, it will also generally imply that policy should be *state-contingent* as well. For example, in the policy problem considered by Eggertsson and Woodford (2003), the optimal policy involves keeping the nominal interest rate at its lower bound for several quarters even after the natural rate returns to its normal level; but the *exact number* of quarters for which this should be done depends on the evolution of the exogenous disturbance, and is not known until date T is reached. Moreover, the fact that, in the particular numerical exercise considered in Figure 1, it is possible to make a definite commitment once period T is reached depends on the fact that there is assumed to be no further uncertainty about the evolution of fundamentals after date T . In the case of a more general disturbance process $\{r_t^n\}$, the number of periods for which interest rates should be kept low will also depend on the path of the natural rate *after* it has again become positive; under an optimal policy, the central bank would not generally know whether it was yet time to raise rates until the time to do so was reached.

The kind of commitment that needs to be communicated, in order to allow a closer approximation to fully optimal policy, is one that would indicate the way in which future policy should depend on future economic developments. This might seem so complex as to not be usefully explained to the public; but my own view is that even a very general indication of the kind of factors that should be crucial for future policy decisions would greatly help to clarify the public's view of the likely state-contingent evolution of interest rates and of the economy. In the context of the simple policy problem considered above, Eggertsson and Woodford show that the optimal time and degree to which interest rates should eventually be raised can be explained in terms of a fairly simple formula. Under the policy rule that they propose,²⁰ the central bank should set its policy rate so as to achieve a particular pre-announced target level for an output-gap-adjusted price-level target,²¹ to the extent that this is consistent with

²⁰Other approaches to the implementation of the optimal state-contingent policy in a similar model are discussed by Svensson (2004) and by Sugo and Teranishi (2005).

²¹This variable is equal to the log price level plus a positive multiple of the output gap. Thus the price level target is automatically increased slightly in the event of a negative output gap.

the interest-rate lower bound. The interest rate will thus be kept at the lower bound *as long as it continues to be impossible to reach (or exceed) this target*, even with interest rates at the lower bound; rates should be raised above the lower bound once the target level for the output-gap-adjusted price level is reached, and not sooner. A commitment of this kind would *imply* that the lower-bound policy should be expected to continue for a considerable period, in the case that the output-gap adjusted price level is currently well below the target; and a policy commitment that emphasized this target (and hence the size of the gap that would remain to be closed at any given time) would even allow the private sector some basis for judging the likely length of such a period. But it would also automatically imply that increases in interest rates would likely be appropriate soon, as the gap with respect to the target shrank, and would furthermore provide guidance as to how policy should be expected to be conducted thereafter, all without any need for a change in the language of the commitment. And it would be a form of commitment that would make evident the state-contingency of the implied path of interest rates.

The FOMC has made some effort to communicate the contingent nature of its statements about the outlook for future policy. In December 2003, the statement that rates were likely to remain low for a “considerable period” was explicitly linked to the observation of “inflation quite low and resource use slack.” According to the minutes of the January 2004 meeting, this language had been intended to “underscor[e] the notion that a move away from the current degree of policy accommodation would depend on economic conditions rather than simply on the passage of time.” These minutes also indicated that the language adopted in the statement released after the January meeting, referring to “patience” rather than to a “considerable period,” was intended to indicate more clearly that an increase in interest rates later in the year was possible, “and to underline that any such decision would be made on the basis of evolving economic conditions.” While the reference to “patience” itself may have been a rather cryptic way of indicating that policy would be state-contingent, the eventual publication of the minutes would have made this clearer; and the current policy of expedited release of the minutes makes the possibility of clarifying the state-contingent character of future policy through the minutes, rather than through the post-meeting statement itself, a realistic possibility.²²

²²Governor Kohn (2005) lists as an important reason for the earlier release of the minutes the desire to “help spell out the linkage the Committee may see between any policy inclination and its

It would likely be desirable for the FOMC to experiment further with clarifications of this kind. As the period in which regular quarter-point interest-rate increases at each meeting were fully predictable comes to an end, it will become more important for the FOMC to attempt to communicate about the state-contingent character of policy, if it is to comment on future policy at all. Recent experience suggests that comments on future policy can help, both in reducing the number of policy surprises and in keeping bond-market expectations in line with the FOMC's own outlook for rates over the medium term, and these indications of success in steering expectations should increase the effectiveness of policy. But a continuation of this success under more normal circumstances will require the development of more flexible ways of speaking about the likely character of future policy.

3 Assumptions About Future Policy in Inflation-Forecast Targeting

Probably the most important advances in communications policy over the past ten to fifteen years have been made by the inflation-targeting central banks, among which banks such as the Sveriges Riksbank, the Bank of England, and the Reserve Bank of New Zealand have been especially important innovators in the development of new methods of communication with the markets and the general public. The Inflation Reports of these banks provide good practical examples of communication with the public about the central bank's policy commitments. These reports do not pretend to give a blow-by-blow account of the deliberations by which the central bank reached the position that it has determined to announce; but they do explain the *analysis* behind the decision that has been reached. This analysis provides information about the bank's systematic approach to policy by illustrating its application to the concrete circumstances that have arisen since the last report; and it provides information about how conditions are likely to develop in the future through explicit discussion of the bank's own projections. Because the analysis is made public, it can be expected to shape future deliberations; the bank knows that it should be expected to explain why views expressed in the past are not later being followed. Thus a commitment to transparency of this sort helps to make policy more fully rule-based, as well as economic outlook" and "convey the conditionality of Committee thinking."

increasing the public’s understanding of the rule.

The periodic publication of Inflation Reports is a key element in the kind of policy regime that Svensson (1999) calls “inflation-forecast targeting.” Under this approach, the central bank does not only announce a quantitative target (its inflation target) that defines the goal of policy. It is also committed to a particular kind of decision procedure, under which projections are made of the future evolution of inflation and other variables under a particular assumed stance of policy, and the assumed policy is to be implemented (until the matter is reconsidered in the next decision cycle) only if the projections satisfy a certain target criterion. For example, in the case of the Bank of England, the criterion given primary emphasis (at least in the public justification of the policy decisions that are taken) is one that requires projected CPI inflation to equal 2.0 percent at a horizon eight quarters in the future.²³ And finally, it explains its policy decisions to the public in terms of their conformity with the target criterion. In the case of the central banks just mentioned, this means the publication of Inflation Reports several times per year, that give prominent attention to the projections that justify the current stance of policy.

While the development of inflation-forecast targeting represents a substantial advance, both in the commitment of central banks to the conduct of policy in accordance with an explicit rule and in the transparency of communication with the public about policy deliberations, the precise techniques that are used continue to be refined. One of the most debated aspects of current practice has been the question of what kind of assumption to make about the *future* conduct of policy when preparing the projections that will be used to judge the appropriateness of *current* policy.

3.1 Constant-Interest-Rate Projections

Computation of projected paths for variables such as inflation and output some years into the future requires that one make assumptions about the future conduct of monetary policy — at least over the horizon of the projection, and, in the case of a model of the transmission mechanism that incorporates forward-looking behavior by the private sector, even farther. This is a particularly delicate aspect of such exercises,

²³Before 2004, the criterion required the projection of a different inflation measure, RPIX inflation, to equal 2.5 percent at the 8-quarter horizon (Vickers, 1998; Goodhart, 2001). The change in target criterion is discussed in Bank of England (2004a).

because of the implied need for the central bank to take a stand on the question of how it is likely to conduct policy in the future, and even more critically, because of concern that public discussion of the assumptions being made could be interpreted as a statement of the bank's intentions. Statements of intentions regarding future policy have often been regarded as problematic, for reasons of the kind already discussed above.

A common way of seeking to avoid any statement about future policy has been to base policy deliberations — or at least, the way these deliberations are presented in the banks' Inflation Reports — on projections of the future evolution of inflation and other variables under an assumption that the interest-rate target (repo rate) will remain *constant* over the horizon of the projection, at the level that is chosen currently. (This was, for example, the assumption made in the base-case projections that were presented in the overview section of the Bank of England *Inflation Reports*, prior to August 2004; and it is still the assumption made in the base-case projections in the *Inflation Reports* of the Sveriges Riksbank.) The policy decision is then a search for an interest rate with the property that constant-interest-rate projections assuming that particular rate satisfy a particular target criterion (for example, projected CPI inflation of 2.0 percent two years in the future).²⁴ The Inflation Reports then justify the interest-rate decision that has most recently been made by presenting these projections and noting that they conform fairly well to the criterion in question.

This way of avoiding any need for the central bank to show its cards with regard to future policy has the advantage of being simple to explain to the public — as long as the public is not sophisticated enough to ask what it really means — but has a number of unappealing implications.²⁵ First of all, many optimizing models of the monetary transmission mechanism have the property first demonstrated by Sargent and Wallace (1975) for a rational-expectations IS-LM framework, namely, that the equilibrium path of the price level (and hence of the inflation rate) is *indeterminate* under the assumption of a fixed nominal interest rate (or indeed, any exogenously

²⁴Former Bank of England MPC member Charles Goodhart (2001) describes himself as having tried to set interest rates in this way, and says “This was, I thought, what the exercise was supposed to be” (p. 177). Jansson and Vredin (2003) describe the similar procedure used by the Sveriges Riksbank.

²⁵Goodhart (2001) reviews what he calls “the prima facie case against” this approach before offering his defense of it. Other critical discussions include Leitemo (2003), Svensson (2003), and Honkapohja and Mitra (2003).

specified interest-rate process).²⁶ If such a model were to be used for the central bank’s projection exercise, the staff would be unable to compute predicted paths for inflation or other variables under the hypothesis of any constant level of nominal interest rate, and so unable to assert that one particular level would imply satisfaction of the target criterion.²⁷

Alternatively, many backward-looking models (including optimizing models in which expectations are assumed to be based on extrapolation from past time series) have the property discussed by Friedman (1968), namely, that maintaining a constant nominal interest rate indefinitely will lead to explosive inflation dynamics, through a Wicksellian “cumulative process.”²⁸ Goodhart (2001) suggests that the Bank of England’s model has this latter property, and that as a result, “the rate of change of most variables visible at the two-year horizon in the Bank’s forecast generally (though not invariably) tends to persist, and on occasion to accelerate, in the third and subsequent years” (p. 171).²⁹ An example of this property is shown in the box on pp. 42-43 of the August 2004 *Inflation Report* (Bank of England, 2004b), where the constant-interest-rate inflation projection from the February 2004 report is extended another year into the future. While the projection showed CPI inflation rising to about 2.0 percent, under the most likely scenario, by early 2006, it showed inflation continuing to rise, to about 2.4 percent, by early 2007, with no indication of convergence even at that level. In this case, it is possible to ask which constant interest rate would imply satisfaction of the target criterion at a certain finite horizon, but

²⁶See Woodford (2003, chap. 4) for further discussion.

²⁷Leitemo (2003) discusses possible interpretations of the constant-interest-rate projection exercise that would allow it to yield a policy recommendation even in the case of a forward-looking model of the transmission mechanism; but these do not eliminate the other unappealing features of such a procedure.

²⁸See Bullard and Mitra (2002) and Preston (2005) for analyses of forward-looking models with least-squares learning by the private sector.

²⁹Goodhart (2005) indicates that “in medium run simulations at the Bank of England running much beyond [a] two-year horizon, the constant two-year rate assumption had to be linked into a Taylor-type reaction function to prevent nonsensical trends from developing as the horizon extended beyond two years (p. 7).” Goodhart argues that this does not present any problem for an exercise in which the constant-rate assumption is maintained only over a two-year horizon. But if one admits the acceptability of imposing a reaction function as the policy assumption beyond the two-year horizon, it is unclear why one should not be willing to impose a reaction function for earlier dates as well, at least to the extent that the MPC is not willing to take a stand on a particular direction of likely near-term deviation from the ‘typical’ reaction function.

only at the expense of making it clear that hitting the target at (say) the 8-quarter horizon does *not* also imply expecting to hit it in subsequent quarters. Hence it cannot be the case that one expects to be content to maintain the constant-interest-rate policy indefinitely, even in the absence of any developments that cannot already be foreseen.

Moreover, if one's model currently implies that inflation will depart significantly from the target rate at the three-year horizon if interest rates are maintained at their current level for that long, then it also implies that one should expect that a year from now — barring unforeseen developments — if interest rates have been maintained at their current level, it will then be forecasted that inflation will depart from the target at the *two-year* horizon if interest rates are not changed. For example, in the case just mentioned, the projection in February 2004, based on an assumption that the repo rate would remain at 4.0 percent over the following three years, implied showed CPI inflation accelerating to about 2.4 percent by early 2007. But this projection would then imply that under the most likely scenario, keeping the repo rate at 4.0 percent throughout 2004 would be expected to result in the Bank's projecting in February 2005 that CPI inflation should reach 2.4 percent in only two years, at which point (if not sooner), the exercise should require the repo rate to be raised. Thus the projection would imply that one should *not* expect the repo rate to remain at its current level for an entire year, even in the absence of any "news". It should have been expected to be raised fairly soon, as indeed it was (by 75 basis points over the next six months).

The publication of constant-interest-rate projections — and the public justification of policy decisions by reference to them — is in no way intended to suggest that the central bank intends to maintain interest rates constant over the period of the projection. (Indeed, the most important justification for the use of constant-interest-rate projections seems to be a desire *not* to express any intention regarding future policy.) Nor can it be defended as representing the central bank's own best current estimate of the future path of interest rates; after all, the implication of the projections explained above would be evident above all within the central bank itself.³⁰

³⁰Even before the Bank of England ceased to use the constant-interest-rate projections as the base case in its *Inflation Report*, it was fairly clear that these projections did not represent the Bank's own forecast of how the economy was most likely to evolve. This was conceded at least implicitly in the Bank's published discussions of the accuracy of its projections, for example in the *Inflation*

But this implies that the targeting procedure is based on forecasts that are not actually believed, even in the central bank itself. Such a procedure has the paradoxical implication that the central bank may choose a policy under which it does *not* truly expect the target criterion to be satisfied, though it may believe that it would be under the counterfactual hypothesis of the constant interest rate.³¹ Such a state of affairs can hardly be defended as conducive to transparency in the conduct of monetary policy. If policy is genuinely based on constant-interest-rate conditional projections, then one's policy decisions are not aimed at ensuring satisfaction of the target criterion that is announced to the public; and the projections published by the central bank are not accurate forecasts that should better help the private sector to correctly anticipate the economy's evolution. On the other hand, if the central bank genuinely does expect the target criterion to be satisfied, then policy is not actually determined in the way that the official rhetoric implies that it is; and if the forecasts are unbiased, then they are not the kind of forecasts that they are officially described as being.

The kind of forecast-targeting procedure recommended by Svensson and Woodford (2005) as a way of implementing optimal monetary policy is of a different sort. In this procedure, one projects the economy's future evolution under alternative contemplated policy decisions, assuming that in future decision cycles the central bank will *again act to ensure satisfaction of the target criterion*. This amounts to asking what

Reports of August 2001 and August 2002. In these discussions, the Bank gave exclusive attention to the projections that it also published in which an interest-rate path was assumed corresponding to current market expectations, rather than to the projections conditional on the constant interest-rate path. If the Bank regarded the constant-interest-rate assumption as the best available forecast of its behavior, it would want to test the accuracy of the projections made under that assumption, rather than under contrary assumptions that might be made by traders in financial markets.

³¹In the case of the February 2004 projections of the Bank of England already discussed above, the constant-interest-rate projection used as the main basis for policy deliberations at the time indicated inflation near 2.0 percent at the 8-quarter horizon, but surging above two percent over the next year. As shown in the Bank's subsequent discussion of its decision to de-emphasize the constant-interest-rate projections (Bank of England, 2004b, pp. 42-43), a projection based on market anticipations regarding the future path of interest rates (according to which interest rates would soon be raised above the 4.0 percent decided upon in February) instead implied that inflation should remain well below two percent over the entire two-year period, though this projection would imply an inflation rate nearing two percent if extended three years into the future. If the latter projection were really the one regarded as more realistic by the MPC in February, this would imply that they were not really basing their decision on projected inflation at the 8-quarter horizon.

action is needed in order to project that the criterion should be satisfied in the current period, taking as given that it is expected to be satisfied in later periods (as a result of the policy actions to be taken in those periods). Such a calculation yields a determinate outcome as long as there is a determinate rational-expectations equilibrium implied by the target criterion; this is always the case if the target criterion is selected according to the method of Giannoni and Woodford (2002).

Thus I would argue that policy should be based on a projection exercise that includes a model of the central bank's own future behavior — one that is furthermore consistent with the procedure that it actually follows in making its policy decisions. This is the kind of projection exercise used as the basis for policy decisions at some central banks, notably the Reserve Bank of New Zealand, which also publishes some information about the non-constant interest-rate path implicit in its projections, along with its projections for inflation and other variables.³²

Goodhart (2001, 2005) objects that such a procedure is impractical, on the ground that it would be much more difficult for a monetary policy committee to reach agreement on an entire future path for interest rates, rather than allowing them to decide only about the current interest rate each time they meet. But the procedure described by Svensson and Woodford does not involve a multi-dimensional decision problem in each decision cycle. As with the constant-interest-rate projection method, one makes a decision for the current period only, on the basis of projections of the future that (necessarily) incorporate a hypothesis about future policy; the hypothesis about future policy is simply a more realistic one than the notion that interest rates will not change, regardless of how inflation and output evolve. And there is no greater need for agreement among the members of the policy committee about that particular aspect of the model specification than about the other assumptions involved in making projections for the future.³³

Goodhart also argues that revealing a projected non-constant path for interest

³²The models used at some other banks, such as the Bank of Canada, similarly include equations intended to represent future policy; but these banks do not publish their projections.

³³The members of the monetary policy committee *might* wish, under certain circumstances, to modify the model's default rule for the future conduct of policy because they do not regard it as correctly representing their intentions regarding near-term future policy. But this would only occur to the extent that it was in fact possible for them to agree that current conditions would justify a departure from typical policy, as in the case of the recent response to the perceived threat of deflation in the U.S., discussed above.

rates is problematic, because “any indication that the MPC is formally indicating a future specific change in rates ... would be taken to indicate some degree of commitment” (2001, p. 175).³⁴ This is clearly a delicate issue in the proper explanation to the public of how the central bank’s projections are to be interpreted. Yet the danger is not as great in this case as in the case of the signals regarding future policy that have recently been included in the post-meeting statements of the FOMC in the U.S. For as has just been noted, the MPC would not have to decide on a forward path for interest rates, that is then fed into the bank’s model in order to generate the projections; instead, the model could incorporate an equation representing typical policy. The resulting projections would include a path for the policy rate, and to the extent to which the MPC announced that this projection represented its best judgment about how the economy was likely to evolve, it would be endorsing a forecast of its future decisions. But it would be fairly easy in this case for the discussion of the projections to include a disclaimer stating that the interest-rate projection is not intended to pre-judge the policy decisions that the MPC will actually make at later dates.

And the experience of New Zealand suggests that it is possible to reveal interest-rate projections to the public without being understood to have made an advance commitment about the path of the official cash rate. Archer (2004) discusses the RBNZ’s experience with the publication of a forward path for interest rates. While he mentions the possibility of the projected interest rate path’s being misinterpreted “as a policy plan” (p.9), this is cited as a concern expressed to him by other central bankers, rather than as a problem that has arisen in practice in New Zealand. The main practical problem that he cites with regard to the publication of an interest-rate path is that it has not always been possible to produce a model-based projection that coincided with the policymaker’s assessment of the likely future path of interest rates, in which case the quantitative projection and the discussion of future policy in the Monetary Policy Statement do not agree with one another. According to Archer, “it is noteworthy that on all such occasions, market analysts and position takers expressed frustration at the inconsistency” between the two contrasting messages regarding future policy (p. 10). The problem in such cases has been a failure of policymaker confidence in the assumptions reflected in the model-based projection. It is not clear why this problem should be greater in the case of projections regarding

³⁴See also Goodhart (2005, p. 6).

the path of interest rates than with other variables, though central banks may well be especially careful about what they say about this particular aspect of the future outlook.

Moreover, a “fan chart” for the path of interest rates ought to make it clear that the bank is not committing itself to a definite path; rather, the expected evolution will depend on a variety of contingencies that can at best be assigned probabilities. The practical possibility of communicating about this kind of uncertainty is illustrated by the way that the Bank of England currently discusses the interest-rate assumptions used in its projections “based on market interest-rate expectations.” When explaining the particular interest-rate path that is assumed in the projections, the *Inflation Report* always takes care to note that “there is a high probability that official interest rates will not follow this path Given the great uncertainties, the economy will almost certainly not evolve in the way either the MPC or the markets expect,” and a fan chart is presented indicating the degree of market uncertainty about interest rates at progressively longer horizons, based on the prices of options on futures contracts.³⁵ The fan chart would seem an effective device for communication about the uncertainty around the published interest-rate path. In the case of an interest-rate path implied by a quantitative model augmented by a policy equation, it would be possible to generate the probability distributions that are plotted in the fan chart in the same way as the fan charts for inflation and output are currently generated.

3.2 Projections Based on Market Expectations

The Bank of England has evidently accepted the force of at least some of the criticisms of the use of constant-interest-rate projections, and since the August 2004 *Inflation Report* it has ceased to emphasize those projections in its justification of current policy. But rather than adding a policy equation to its model, as is done in New Zealand, it now focuses its evaluation of policy on a set of projections that are conditional on the path of short-term interest rates implied by the term structure of yields on longer-term Treasury securities.³⁶ This allows the projections to be based

³⁵See, for example, Chart 6.1 in Bank of England (2004b, p. 41); the quotation in the text is from the same page.

³⁶The Sveriges Riksbank has also begun, in its 2005:Q1 *Inflation Report*, to give more prominence to projections conditional on an interest-rate path inferred from the term structure. However, the Riksbank continues to base its “main scenario” on the assumption that the repo rate will remain

on a more realistic assumption regarding future interest rates, while still allowing the MPC to remain silent as to whether the interest-rate assumptions used in the projection exercise agree with their own.³⁷ The way in which these projections are used in the MPC's decision procedure has not been explicitly discussed. Apparently, the idea is that if the projections based on market expectations satisfy the target criterion, then the MPC should set the repo rate at the level *expected by the markets*. Thus in August 2004 the rate was raised from 4.50 to 4.75 percent, to conform to market expectations of a repo rate averaging 4.6 in 2004:Q3 and rising to an average of 4.9 in 2004:Q4. In November 2004, it was left unchanged, because market expectations at this time forecasted only an average of 4.7 in both 2004:Q4 and 2005:Q1; and in February 2005, it was again left unchanged, because this continued to be what the markets expected.³⁸ If the projections based on market expectations were to fail to satisfy the target criterion, then presumably policy should deviate from the market expectation, though it is not clear by how much; this situation appears not yet to have arisen.

While this alternative avoids some of the problems associated with constant-interest-rate projections, it does not avoid all of them, and introduces some new problems of its own.³⁹ The problems of inconsistency that arise when policy deliberations (or at least the public justification of these deliberations) are based on an interest-rate assumption different from what the MPC believes is most likely to occur remain, as long as the assumed path does not actually represent the MPC's forecast. The new approach makes the contradiction less glaring, since it is no longer obvious in which particular way the MPC should be expecting something different from what is assumed. But if the MPC *does* disagree with the assumed interest-rate path, the procedure is still incoherent and/or misleading; and it is hard to see how continued

unchanged. The alternative scenario is also presented, late in the report, to "provide a broader base for discussions of monetary policy" (Sveriges Riksbank, 2005, p. 5), but is not referred to in the main discussion of inflation risks under current policy.

³⁷The explanation of the interest-rate assumption includes the following qualification: "It is important to stress that the market rate path does not represent the MPC's forecast of official interest rates.... Financial markets may judge economic prospects differently from the MPC" (Bank of England, 2004b, p. 41).

³⁸See Table 6.A, "Market expectations of the Bank's official interest rate," in each of these issues of the *Inflation Report*.

³⁹See also Goodhart (2005) for criticism of the new procedure.

coyness of the MPC as to whether it agrees or not with its stated assumptions can serve the goal of clarifying the way in which policy is conducted.

The problem that the interest-rate assumption would not allow an equilibrium path to be computed, in the case of a standard forward-looking model, or would imply unstable dynamics, in the case of many backward-looking models, is also not avoided by the new proposal. These problems arise whenever *a path for the nominal interest rate is assumed*, that is independent of the evolution of the endogenous variables in the model; they have nothing to do with the *constancy* of the assumed path. When a particular path for interest rates is inferred from the term structure and plugged into a model of the monetary transmission mechanism as if it were given exogenously, the same problems will arise as in the case of a constant-interest-rate assumption. (Even if nominal interest rates are assumed to rise over the coming year, the fact that they are assumed to rise by an amount independent of any increase in inflation gives rise to unstable dynamics: higher inflation will lower the real interest rate, stimulating higher inflation, and so on.) The only solution for this problem is to include in one's model a realistic representation of *endogenous* variation in short-term nominal interest rates.

At the same time, a decision procedure using projections based on market expectations introduces some new problems. Most importantly, it runs the risk of making policy too sensitive to market expectations regarding policy, in a way that fails to provide any anchor for those expectations or any stable course for policy. Consider an extreme version of the approach to policy sketched above, in which the central bank simply infers market expectations regarding the path of its policy rate, and sets the rate in accordance with market expectations. As Blinder (1998) points out, "following the markets" in this way would be quite dangerous, for there would then be no reason for the markets to expect one kind of policy rather than any other; arbitrary notions could easily become self-fulfilling, and the sources of significant instability and/or inefficiency.

Of course, the approach to policy that has apparently been adopted by the Bank of England is more sophisticated than that; there is no commitment to follow the markets' lead, unless the Bank's projections imply that doing so is consistent with a projection of inflation near two percent two years in the future. But it is not clear to what extent such a qualification should succeed in preventing fluctuations due to self-fulfilling expectations. This is because, even when arbitrary fluctuations of that

kind occur, inflation may still be (correctly) predicted at any point in time to revert back to its target level within a few quarters.

As an example, consider the simple model of the monetary transmission mechanism discussed above, according to which inflation and output are determined each period by equations (2.1) and (2.2). Let s_t be an exogenous random process that has no relation to economic “fundamentals”⁴⁰ — what is sometimes called a “sunspot” variable — and suppose that its dynamics can be described by a first-order autoregressive equation,

$$s_t = \rho s_{t-1} + \epsilon_t, \quad (3.1)$$

where $0 < \rho < 1$ is the coefficient of autocorrelation and $\{\epsilon_t\}$ is a bounded white-noise disturbance. I wish to consider the possibility of an equilibrium in which inflation and output fluctuate in response to variation in the sunspot variable, simply because people have come (for arbitrary reasons) to expect this, and have observed that the variable does indeed help them to forecast the economy’s future evolution. Consider, for example, the possibility of an equilibrium in which

$$\pi_t = \phi s_t,$$

for some coefficient $\phi \neq 0$. Equation (2.1) will be satisfied as long as the equilibrium fluctuations in the output gap are given by

$$x_t = \frac{1 - \beta\rho}{\kappa} \phi s_t.$$

Equation (2.2) will also be satisfied as long as the nominal interest rate satisfies

$$i_t = r_t^n + \left[\rho - (1 - \rho) \left(\frac{1 - \beta\rho}{\kappa} \right) \sigma^{-1} \right] \phi s_t. \quad (3.2)$$

Now suppose that in each period t , the exogenous state of the world (including the current values of r_t^n and s_t) is first revealed; then futures markets are open, in which traders bet on the value of that period’s interest rate i_t ; and finally, the central bank chooses its operating target for i_t , after learning the market forecast $i_{t|t}$ implied by the futures prices, and period t inflation and output are then determined

⁴⁰In particular, it is unrelated to the real factors that cause variation in either the natural rate of output or the natural rate of interest.

in accordance with equations (2.1) – (2.2). In the equilibrium just conjectured, the market expectation should be given by

$$i_{t|t} = r_t^n + \left[\rho - (1 - \rho) \left(\frac{1 - \beta\rho}{\kappa} \right) \sigma^{-1} \right] \phi s_t.$$

If the central bank observes this, and sets $i_t = i_{t|t}$, then (3.2) will be satisfied, and the equations given above for inflation and output will represent a rational-expectations equilibrium.

But should the central bank be willing to follow the markets and set $i_t = i_{t|t}$? In the equilibrium just described, a correct forecast of the future path of inflation will in any period be given by

$$E_t \pi_{t+j} = \rho^j \phi s_t,$$

for arbitrary $j \geq 0$.⁴¹ If the central bank forecasts in this way, conditional on policy that coincides with market expectations, it will conclude that the inflation rate should converge back to its long-run target value (here assumed to equal zero⁴²) as the horizon j is extended farther into the future; and this will be true no matter how large ϕ is, and hence no matter how large the short-run fluctuations in inflation and output due to self-fulfilling expectations may be. Furthermore, if ρ is not close to 1, the convergence will be predicted to be nearly complete after only a few quarters.⁴³ It is thus not obvious that a central bank that pays attention only to the projected

⁴¹Substitution of the interest rate path $\{i_{t+j|t}\}$ expected by the markets into the model consisting of equations (2.1) – (2.2) would not yield this as the only possible equilibrium, because of the indeterminacy problem already referred to in the case of any exogenously specified interest-rate path. But it would be *one* possible projection consistent with both the model and with market expectations regarding the path of interest rates; and since it is the *correct* forecast, in the conjectured equilibrium, I shall suppose that the central bank is sophisticated enough to produce this forecast.

⁴²For simplicity, I here assume that the target inflation rate is zero. This allows me to avoid discussing the question whether it makes sense to suppose, as in the Calvo pricing model used here, that prices should remain fixed in nominal terms between the occasions on which they are re-optimized, even when the central bank's target rate of inflation is positive and inflation is positive on average. The point made here about the possibility of sunspot equilibria in which inflation reverts quickly to the target level would be equally valid if the target rate of inflation were assumed to be positive.

⁴³For example, in the case that $\rho = 0.7$ and periods represent quarters, one could have an equilibrium in which actual inflation varies over a range as wide as 6 percentage points (3 points above and below the target), solely as a result of self-fulfilling expectations, but in which projected inflation 8 quarters in the future would never be more than 10 basis points away from the target.

inflation rate two or more years in the future would find any reason not to follow the markets at all times, even if this policy allowed large transitory fluctuations in inflation (and associated large swings in output relative to potential) to occur, due solely to self-fulfilling expectations.

One might argue that in the case just described, the possibility of fluctuations in response to the sunspot disturbance would be eliminated as long as the central bank were to establish a reputation for responding to even small departures of the projected inflation rate two years in the future from the target value. For example, if the central bank were to commit itself to a rule of the form

$$i_t = i_{t|t} + \psi \hat{E}_t \pi_{t+8}, \quad (3.3)$$

for some coefficient $\psi > 0$, where $\hat{E}_t \pi_{t+8}$ represents the central bank's projection of inflation 8 periods in the future, conditional on its conducting policy in the way anticipated in the futures markets, then the only possible rational-expectations equilibrium would have to be one in which $E_t \pi_{t+8} = 0$ at all times. This would preclude any equilibrium of the kind conjectured above, except the one with $\phi = 0$. However, this result depends on assuming that the central bank would respond systematically (albeit to only a small extent) to even small departures from satisfaction of its target criterion, which seems unlikely given that the policy rate is ordinarily moved only in discrete steps. More to the point, even rule (3.3) would allow the existence of sunspot fluctuations of arbitrary amplitude, in the case of a sunspot variable s_t that evolved as an MA(7) process (or any lower-order MA process), so that $E_t s_{t+8} = 0$ at all times.

Another problem with the current procedure of the Bank of England is that it is unclear how the MPC is intended to determine the correct current repo rate in the event that the interest-rate path expected by the markets is judged to imply projections inconsistent with the Bank's target criterion. Would an attempt be made to determine the current repo rate that would lead to an acceptable projection, under the assumption that *the path of the repo rate after the current month would follow the path anticipated by the markets?* This would typically require an extreme adjustment of the current repo rate, as a change in the repo rate for only one month would have to change the path of inflation over the following two years by enough to get the projected inflation rate two years in the future on track. A more sensible approach would surely involve adjusting the entire path of interest rates to one that the MPC would view as more sound, rather than acting as if the committee expected itself to

behave in the future in the way currently anticipated by the markets, even though it was planning to depart substantially from the markets' expectation in the short run. But in this case, projections would have to be produced on the basis of an assumption about future policy other than the one corresponding to market expectations. The idea that the MPC would be able to avoid taking a stand (at least in its internal deliberations) on a reasonable future path of interest rates, by insisting on using the markets' forecast in its projections, is not tenable.

Thus there seems no coherent alternative to an approach to inflation-forecast targeting in which the central bank's projections are produced on the basis of an assumption that the MPC is willing to make about the way in which its own future policy should endogenously respond to alternative possible future conditions. This need not involve an attempt to determine in advance the actual future path of interest rates (except, of course, in a "central case" scenario that is understood to be unlikely to actually occur), and the central bank might or might not wish to reveal much about the interest-rate path implicit in its projections for other variables. My own view is that communication about this path can help to facilitate the transmission mechanism of policy. For example, Archer (2004) concludes that the slope of the path announced by the RBNZ has effected the slope of the market yield curve in New Zealand, and an ability to influence the expectations reflected in the yield is exactly what a central bank should wish, as argued in section 1. But even if a central bank were to wish to communicate less about this aspect of its deliberations — and it must be admitted that even the RBNZ limits the amount of detail with which it describes the interest-rate path implied by its projections — it should not allow such concerns to prevent it from considering the appropriate character of future policy in its forecast-targeting exercise. And to the extent that it is concerned at all about transparency and accountability, it should not pretend to the public that its deliberations make no assumptions about future policy.

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